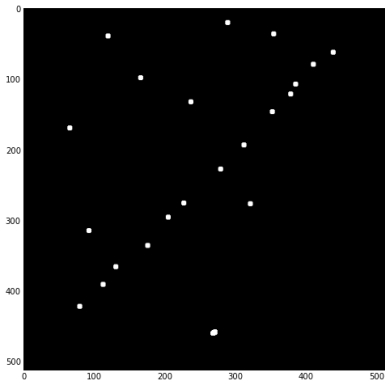


Sample Data for Line Finding

We're going to illustrate the Hough transform for the problem of finding lines in a collection of points.

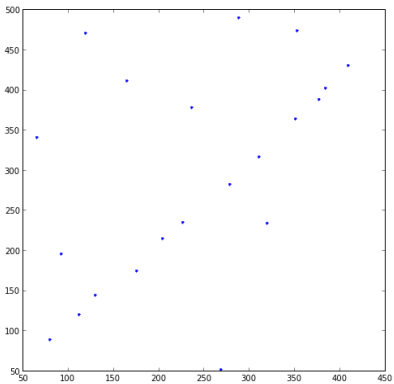
Hough transforms can also be used for more general object recognition problems (see below).

```
1 imshow(imread("points.png"))
```



```
1 image = transpose(imread("points.png")[:,::-1, :, 0])
2 labels, n = measurements.label(image)
3 points = array(measurements.center_of_mass(image, labels, range(1, n))
  )
```

```
1 plot(points[:,0], points[:,1], 'r.')
```



Hough Transform for Lines

The original Hough transform used the following parameterization:

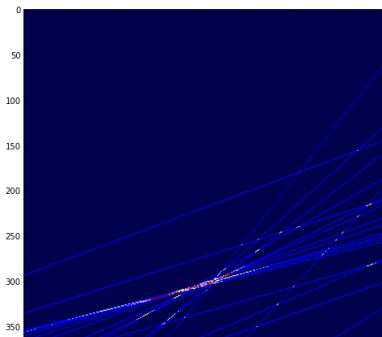
$$y = mx + b$$

The set of parameters corresponding to a point (x,y) is therefore:

$$m = \frac{y - b}{x}$$

Hough space in high resolution

```
1 N = 400; accumulator = zeros((N,N))
2 x,y = points[:,0],points[:,1]
3 for b in range(-200,200):
4     m = (y-b)/x
5     bi = int(b+200)
6     for mi in array((m+2)*100.0,'i'):
7         if bi<0 or bi>=N or mi<0 or mi>=N: continue
8         accumulator[mi,bi] += 1
9 imshow(accumulator , cmap=cm.seismic)
```



Coarse buckets:

The traditional Hough transform uses “bins” or “buckets” for accumulation. That’s similar to downsampling after a box filtering operation.

```
1 N = 20
2 hough = zeros((N,N))
3 x,y = points[:,0],points[:,1]
4 for bi in range(20):
5     b = (bi-10)*20.0
6     m = (y-b)/x
7     for mi in array((m+2)*5.0, 'i'):
8         if bi<0 or bi>=N or mi<0 or mi>=N: continue
9         hough[mi,bi] += 1
10 imshow(hough, cmap=cm.seismic, interpolation='nearest')
```



Probabilistic Hough Transform:

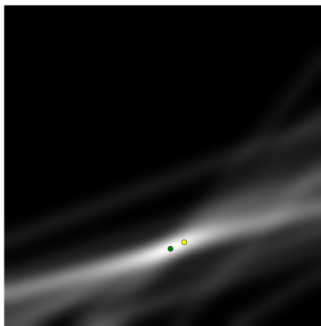
Bucketing is not a very good method for detecting maxima.

It's better to accumulate at a high resolution, convolve with a Gaussian, and then look for the maximum.

That is a technique similar to something called the probabilistic Hough transform.

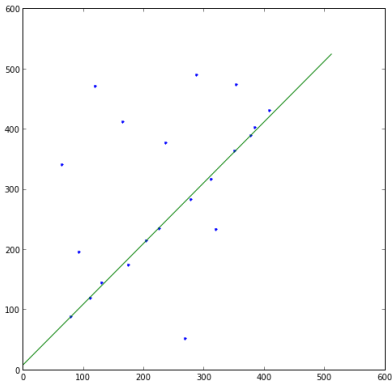
However, a uniform Gaussian convolution is still not entirely justified; the actual convolution needed for a correct probabilistic treatment would have to be spatially non-uniform.

```
1 smoothed = filters.gaussian_filter(accumulator,10.0)
2 axis("off"); imshow(smoothed,cmap=cm.gray)
3 mi0,bi0 = measurements.maximum_position(accumulator); plot([bi0],[
    mi0], 'o',color='yellow')
4 mi,bi = measurements.maximum_position(smoothed); plot([bi],[mi], 'o'
    ,color='green')
```



To identify the actual line, we need to find the bucket containing the maximum and transform back.

```
1 m = (mi-200)/100.0; b = bi-200.0  
2 plot(points[:,0],points[:,1],'.'); plot([0,512],[b,m*512+b])
```



Other Parameterization

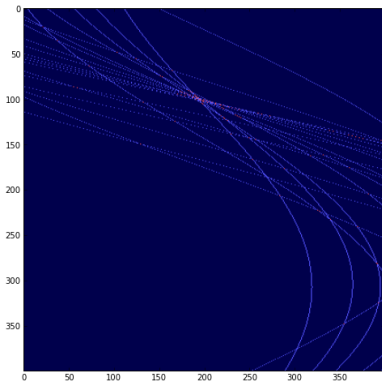
The $y = mx + b$ parameterization is not very good because we can't detect vertical lines.

It is better to parameterize lines by ϕ and d :

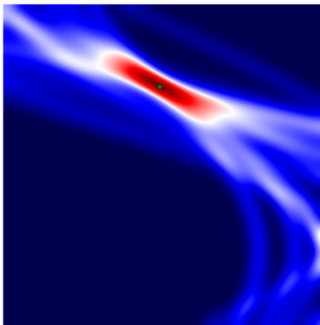
$$x \cos \phi + y \sin \phi = d$$

$$y = \frac{d}{\sin \phi} - x \frac{\cos \phi}{\sin \phi}$$

```
1 accumulator = zeros((400,400))
2 for x,y in points:
3     for p in range(-200,200):
4         phi = (pi/2)*p/200.0
5         d = x*cos(phi)+y*sin(phi)
6         if d<-200 or d>=200: continue
7         accumulator[p+200,d+200] += 1
8 imshow(accumulator , cmap=cm.seismic)
```




```
1 smoothed = filters.gaussian_filter(accumulator,10.0)
2 axis("off"); imshow(smoothed,cmap=cm.seismic)
3 p,di = measurements.maximum_position(smoothed)
4 plot([di],[p],'go')
```



```
1 phi = (pi/2)*(p-200)/200.0
2 d = di-200
3 plot(points[:,0],points[:,1],'.')
4 plot([0,512],[d/sin(phi),d/sin(phi)-512*cos(phi)/sin(phi)],'g-')
```

